High Precision Detection of Change in Intermediate Range Order of Amorphous Zirconia-Doped Tantala Thin Films Due to Annealing

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Understanding the local atomic order in amorphous thin film coatings and how it relates to macroscopic performance factors, such as mechanical loss, provides an important path towards enabling the accelerated discovery and development of improved coatings. High precision x-ray scattering measurements of thin films of amorphous zirconia-doped tantala (ZrO_2-Ta_2O_5) show systematic changes in intermediate range order (IRO) as a function of postdeposition heat treatment (annealing). Atomic modeling captures and explains these changes, and shows that the material has building blocks of metal-centered polyhedra and the effect of annealing is to alter the connections between the polyhedra. The observed changes in IRO are associated with a shift in the ratio of corner-sharing to edge-sharing polyhedra. These changes correlate with changes in mechanical loss upon annealing, and suggest that the mechanical loss can be reduced by developing a material with a designed ratio of corner-sharing to edge-sharing polyhedra.

Amorphous thin film coatings are technologically important materials that often limit the accuracy of a variety of precision measurements. For example, Brownian thermal noise, due to mechanical loss in thin film coatings, is a significant impairment in atomic clocks [1] and interferometric gravitational-wave detectors [2], such as the Laser Interferometer Gravitational-wave Observatory (LIGO), Virgo and KAGRA. It is of critical importance to future generations of interferometric gravitational-wave detectors [3] to develop thin-film coatings with lower mechanical loss, and hence lower Brownian thermal noise. For the Advanced LIGO + upgrade, designed to operate at room temperature and due to start installation in 2022, a coating with a fourfold improvement in mechanical loss is desired, which together with frequency dependent squeezing would enable an eightfold increase in the volume of the Universe observable by gravitational waves [4,5].

Postdeposition annealing of amorphous thin films has been shown to induce changes in both the atomic structure and mechanical loss [6,7]. Annealing tantala up to 600 °C, prior to the onset of crystallization, reduces the room temperature mechanical loss of the coatings [8]. Doping tantala with zirconia can suppress crystallization, allowing thin films to remain amorphous after annealing up to 800 °C [9]. For the zirconia-doped tantala studied here, the mechanical loss of an as-deposited film of $\sim 1 \times 10^{-3}$ significantly decreases to 1.8×10^{-4} upon annealing at 800 °C [10], which is somewhat below the titania-doped tantala currently employed in Advanced LIGO. This result demonstrates that zirconia-doped tantala is a promising coating material system that warrants further study as a potential Advanced LIGO + mirror coating.

The local atomic order in amorphous materials often governs its macroscopic properties, such as mechanical loss. It is therefore of interest to measure the local atomic order, and identify the key atomic structure motifs that govern macroscopic properties. However, obtaining an accurate measurement of the local order is challenging,

especially in thin films. In this Letter, we address this challenge and measure with high precision subtle changes in local order as a function of postdeposition annealing of zirconia-doped tantala thin films. We use grazing-incidence pair distribution function (GIPDF) measurements and atomic structure modeling that captures the local order changes accurately up to 15 Å. Finally, we discuss the implications of this improved understanding of the atomic structure and its relation to our efforts to reduce mechanical loss.

In general, the atomic structure of amorphous materials can be described in terms of short- and intermediate-range order (SRO and IRO, respectively); the long-range order (LRO), characteristic of crystals, is unambiguously absent [11,12]. SRO generally describes the structural order up to the first coordination sphere measured as the first peak in the PDF, which often resembles the amorphous material's crystalline counterpart. For zirconia-doped tantala, we choose, among the various definitions of SRO [13], order up to ~ 2.9 Å, which is where the first coordination polyhedra of the material end. The IRO describes the structural organization that is *intermediate* between the discrete chemical bonds described in the SRO and the periodic lattice described in the LRO. However, the IRO is less well understood than the SRO, and is more dependent on the details of how the material was synthesized or deposited.

The structural changes associated with postdeposition annealing are often observed beyond the first coordination sphere, and lie in the IRO [14]. Even with tools that are best suited to probe the IRO, such as fluctuation electron microscopy (FEM) and x-ray or neutron PDFs, the observed structural changes can be small and difficult to interpret. Accurate atomic modeling is required to capture the small changes in the atomic structure, and probe the IRO in detail.

GIPDF data were collected from thin films of zirconia-doped tantala deposited by MLD Technologies (Mountain View, CA), by ion-beam sputtering (IBS) $Zr/(Zr + Ta) \simeq 0.48$, ~ 590 nm in thickness on fused silica substrates [10]. The target materials were pure metals in a partially pressurized oxygen environment, and the ambient temperature during deposition was less than $100\,°C$. Postdeposition annealing in air of three different samples was carried out at 300, 600, and $800\,°C$. GIPDF data were collected at the x-ray scattering beam line 10-2 at the Stanford Synchrotron Radiation Lightsource (SSRL). This unique GIPDF capability allows us to overcome a significant difficulty in measuring PDFs from thin films: a grazing incidence angle can be chosen that enables the collection of x rays scattered from the coatings and not the substrate while maintaining a relatively high q range of 20.1 Å^{-1}. In addition, there is no destructive sample preparation, ensuring that the observed changes in the measured atomic structure do not result from the sample preparation process, which is especially relevant when looking at small structural changes due to annealing. Further details on the GIPDF data collection method and its merits, in particular pertaining to doped
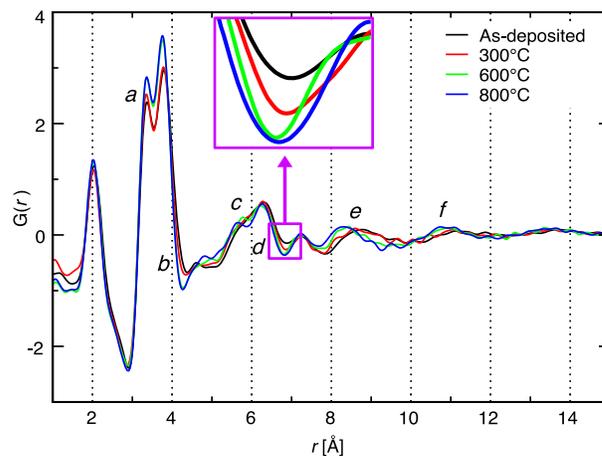

FIG. 1. Detection of annealing induced changes: Measured GIPDFs of zirconia-doped tantala thin films. The thin films differed only in annealing history: as-deposited, 300, 400, 600, and $800\,°C$. The differences among the PDFs are the result of annealing-induced change to the atomic structure. The letters represent sections of PDF where the most significant changes are observed: *a*, *b*, and *d* change in intensity, *c* new peaks appearing, *e* and *f* shift in peak positions. Section *d* is magnified in the inset to highlight the systematic change as a function of annealing temperature.

tantala coatings, are discussed in Ref. [15]. The total scattering data were reduced to the normalized structure factor $S(q)$ after applying identical corrections on all samples for air scattering, absorption, Compton scattering, polarization effects, and geometric effects due to the detector footprint [15–17].

The measured PDFs for an as-deposited sample and the three annealed samples are plotted in Fig. 1. All PDFs show a sharp first peak at 2.0(2) Å, a bifurcated second peak between 2.9(0) and 4.3(0) Å, and a series of smaller peaks between 5 Å and 15 Å. Closer examination reveals a number of changes among the PDFs; the major changes, marked by letters a to f in Fig. 1, lie in the IRO. These include an increase in intensity of the peaks, appearance of new peaks, shifts in the position of the peaks, and a deepening of the troughs. In most cases, the change is *systematic* with respect to the annealing temperature [see inset of Fig. (1)], and remains robust when cutting the q range of the data down to 15 Å^{-1}.

In order to better understand the annealing-induced atomic level processes that cause the changes seen in the PDFs, it is essential to develop atomic models that are accurate enough to capture the observed changes in PDFs. A common method of choice is to follow a regression algorithm that fits atomic coordinates with the measured PDFs, e.g., simulated annealing [18] or reverse Monte Carlo (RMC) modeling [19], etc. However, the changes caused by annealing are subtle even for the two extreme ends of annealing (viz as-deposited and $800\,°C$ annealed) and hence one faces an interesting problem and requirement: how does

one reliably generate two slightly different structural solutions of an otherwise identical disordered system? Conventional modeling techniques often fail to resolve subtle changes in atomic structure with high fidelity, especially in the IRO, which makes it difficult to give definitive statements about the changes in structure.

We follow an integrated modeling approach that seeks to maximally constrain the solution space by using all *a priori* information. Composition and density measurements were performed on the thin film samples to provide starting points for modeling routines (see Ref. [10]). Melt-quench molecular dynamics (MD) simulations, employing two-body empirical potentials from Refs. [20,21], were performed at the measured composition and density to generate starting configurations for RMC modeling. These configurations are then modified using RMC modeling until the computed $S(q)$ matches with the measured $S(q)$. However, it is well known that a traditional RMC modeling produces nonphysical solutions, even in elemental systems [22]. We used *ab initio* molecular dynamics (AIMD) to generate smaller models (190 atoms) of the same system, and the distribution of bond lengths present in the AIMD models was used as a constraint to the RMC modeling. This was achieved by requiring that the metal-oxygen bond distances lie in the range predicted by the partial PDFs of AIMD models (see Ref. [10]). Furthermore, following the "FEAR" method [23], RMC moves were interspersed with energy minimization moves iteratively until the desired agreement with experiments was obtained. The entire modeling algorithm was repeated to get 1000 independent atomic models corresponding to each of the four samples, i.e., as-deposited, 300 °C annealed, 600 °C annealed, and 800 °C annealed. All the properties reported hereafter are computed by averaging over 1000 models. Figure 2 shows the ability of the models to capture the changes on measured PDF up to 15 Å; to the best of our knowledge, it is the first demonstration that atomic models can capture changes in IRO up to 15 Å with such a high accuracy. It should be noted that the models reported in this work are chemically realistic; i.e., they contain no nonphysical metal-metal chemical bonds. The models have a density and composition that are representative of the IBS coatings. We show that deductions made from the models agree with experiments, and the structural features computed from the models show a systematic trend with annealing temperature. A plot showing the fit of the $S(q)$ and $G(r)$ along with additional information on the modeling method is given in the Supplemental Material [10].

In the following, we present a discussion of the structure of a-Ta_2O_5:ZrO_2 based on the models we obtained. As in many glass-forming materials like silica, the structure of a-Ta_2O_5:ZrO_2 can be described as a three-dimensional network of metal (M)-centered coordination polyhedra that have oxygen (O) atoms at their corners. The M-O correlation gives rise to the first peak, which is followed by a minimum at 2.9 Å that defines the M-O bond cutoff
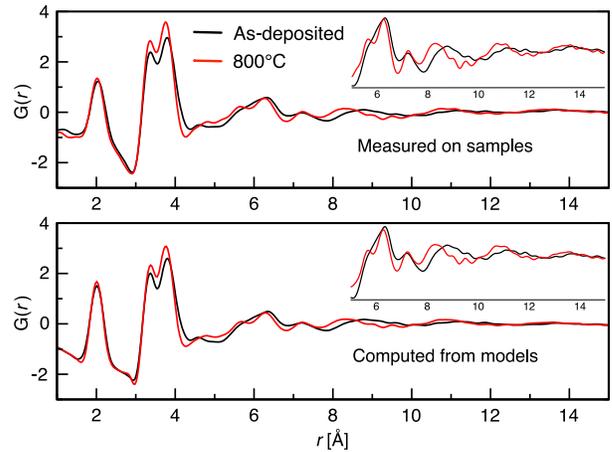

FIG. 2. Measured and computed PDFs: The measured PDFs from two samples (top) are compared with PDFs computed from atomic models (bottom). The PDFs highlight the ability of the atomic models to closely track the annealing-induced changes in the PDFs. Computed PDFs in the bottom plot are averages of over 1000 models. The 5 Å to 15 Å section of the PDFs are shown in higher resolution insets. See Ref. [10] for a plot of all samples.

distance. The polyhedra are predominantly distorted octahedra (~80% for Ta, ~60% for Zr, [10]). It has been shown that the first peak of $G(r)$ for pure a-Ta_2O_5 closely resembles the corresponding peak of crystalline Ta_2O_5 [15]. We find that the coordination of Ta by O (n_{TaO}) is 6.13 whereas n_{ZrO} is 6.14; both values are for as-deposited sample. The measured value of n_{TaO} using ^{17}O NMR studies on IBS deposited pure a-Ta_2O_5 is 6.1(3) [24,25]. The M-O bond distance peaks at 2.0(2) Å and it is comprised of a Ta-O subpeak at 1.98 Å and a Zr-O subpeak at 2.06 Å. The slight difference in Ta-O and Zr-O bond distances is also consistent with *ab initio* models; it is likely that this difference is helpful in frustrating the crystallization of tantala [9]. As a result of annealing, coordination of M by O (n_{MO}) shows a small but consistent trend to smaller values, and a corresponding change, although small, in the M-O bond distance towards a lower value is observed in the total $G(r)$ (see Fig. 10 in Ref. [10]). The structure within the first coordination sphere of tantala has been extensively characterized [6,15,26,27].

The polyhedra link with each other through O atoms at each corner. Each O atom is at least 2-coordinated with metal atoms. The ratio of 2-coordinated to 3-coordinated O atoms is ~1:2, which is notably different from pure tantala where the value measured using NMR is 2:3 [24,25]. The difference comes from O atoms bonding preferentially threefold with Zr; the mean O coordination by M is 2.7 [see inset of Fig. 3(e)]. The correlation between two metal atoms connected by at least one O atom gives rise to the second peak in total $G(r)$. It is interesting to note the bifurcation in the M-M peak into two subpeaks at 3.35 Å and 3.75 Å since similar measurements in pure tantala show the first subpeak at 3.35 Å at much reduced
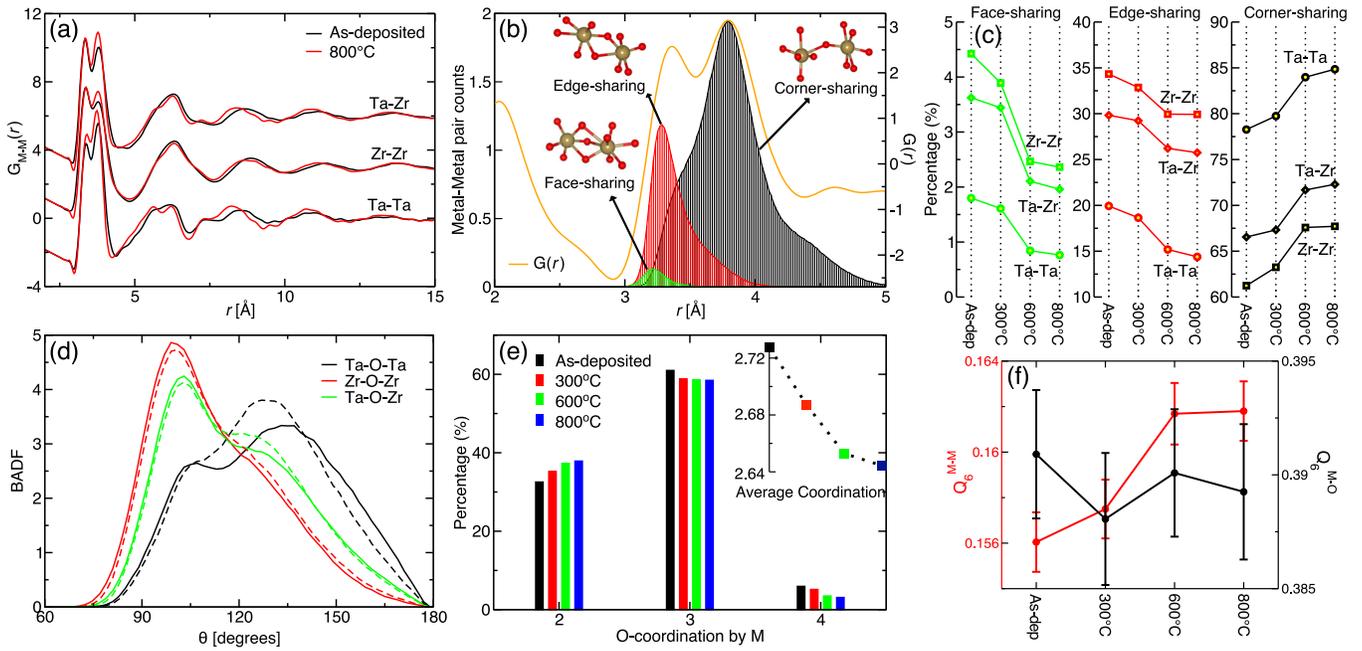
FIG. 3. Structural fingerprints of annealing: The major structural trends observed in the models as a function of annealing temperature are highlighted in (a) through (f): (a) partial $G(r)$ for M-M pairs; (b) origin of the double hump in $G(r)$ as correlations between corner and edge shared M-M pairs, where the orange line represents $G(r)$, and the shaded regions represent the distribution of M-M distances classified as CS, ES, and FS polyhedra; (c) evolution of the percentages of CS, ES, and FS polyhedra; (d) BADF from the as-deposited (dashed lines) and 800 °C annealed (solid lines) models; (e) distribution of O coordination by M for samples with different annealing history, the inset shows the averaged coordination vs annealing temperature; (f) BOO parameters (Q_6) as a function of annealing temperature for M-O and M-M correlations (error bars represent standard deviation).

intensity [15,26]. Its much more pronounced presence in the mixed phase is an effect of doping by zirconia and has structural implications in that the first and second peaks originate from correlations of edge-sharing (ES) and corner-sharing (CS) polyhedra, respectively [Fig. 3(b)]. For the as-deposited sample, the ratio of CS to ES correlations is 3.93 for Ta-Ta, 2.23 for Ta-Zr, and 1.78 for Zr-Zr. There is also a small concentration of face-sharing (FS) polyhedra where the polyhedra share three O atoms between them.

The effect of annealing is more pronounced beyond the first M-O peak and all the way to 15 Å. Many of the changes observed in the total $G(r)$ can be explained by considering the partial M-M correlation [Fig. 3(a)], where changes are observed from ~3 Å up to 15 Å. The peaks become narrower and sharper suggesting that annealing increases the order in M-M correlation lengths. Since the bifurcated M-M peak represents the correlations between the polyhedra, the annealing induced change in the peak signifies that annealing alters the mode by which polyhedra connect with each other. An analysis presented in Fig. 3(c) shows that the concentration of CS polyhedra increases as a result of annealing whereas it decreases for ES and FS polyhedra. The effect of the overall decrease of density of ES and FS polyhedra is that the average O coordination by M decreases as a function of annealing temperature [see Fig. 3(e)]. A decrease in O coordination upon annealing

was also observed for pure tantala using ^{17}O NMR studies in Ref. [25]. An analysis of the M-O-M bond angle distribution function (BADF) shows that the BADF, in general, narrows and shows a more defined peak upon annealing, Fig. 3(d). However, there is a more characteristic change in the BADF: each M-O-M BADF curve shows a double peak and the peak around 120° to 130° increases with annealing. Further analysis shows that the characteristic two-peak BADF arises from the presence of ES and CS polyhedra; the increase in the M-O-M BADF around 120° to 130° is caused by increase in the ratio of CS to ES polyhedra (see Fig. 9 in Ref. [10]).

We use the bond orientational order (BOO) parameter Q_6 [28] to quantify the degree of disorder present in the models. The BOO parameter corresponding to M-O bonds, denoted by $Q_6^{M\text{-}O}$ in Fig. 3(f), shows that there is no significant effect of annealing in the M-O coordination sphere. We also probed the degree of order among the polyhedral units by computing $Q_6^{M\text{-}M}$ among the metal atoms and the values suggest an increase in the BOO with annealing, a trend clearly seen in the measured $G(r)$. To the extent $Q_6^{M\text{-}M}$ is a measure of IRO among the polyhedral units, it is noteworthy to observe an inverse correlation of $Q_6^{M\text{-}M}$ with measured values of mechanical loss at room temperature (see Fig. 1 in Ref. [10]).

A number of experiments have demonstrated that the mechanical loss of tantala-based coatings reduces at

room temperature and increases at low temperature upon annealing [7,8,10,29]. This effect is observed at room temperature for zirconia-doped tantala coatings similar to those studied here, where the mechanical loss undergoes sixfold reduction from $\sim 1 \times 10^{-3}$ in an as-deposited coating to 1.8×10^{-4} when annealed at $800\,°C$. The low temperature mechanical loss of tantala typically produces low temperature loss peaks at around 30 K that develop and grow upon annealing [7], and has recently been observed in other zirconia-doped tantala coatings. The dissipation mechanism for mechanical loss is often conceptualized as two-level systems (TLSs) which are asymmetric double wells separated by an energy barrier. TLSs arise from subtle rearrangements of clusters of atoms [30,31]. The observed trends in mechanical loss with annealing suggests that ES polyhedra are more likely associated with TLSs that contribute to room temperature mechanical loss, whereas the CS polyhedra that form lower barrier height TLSs contribute to low temperature mechanical loss. This conjecture is bolstered by the observation that silica, which has nearly 100% CS polyhedra has low loss in room temperature and high loss at low temperature [32]. If this conjecture is correct, then in order to reduce mechanical loss at room temperature one would seek a material that has fewer ES polyhedra and more CS polyhedra. Conversely, a material with fewer CS polyhedra and more ES polyhedra would reduce mechanical loss at low temperature. As doping with zirconia helps suppress the crystallization but increases the fraction of ES polyhedra, the doping percentage of zirconia is a key variable to optimize in order to reduce mechanical loss at room temperature. In particular, a lower concentration of zirconia that is just enough to suppress the crystallization would be desirable. In a study by Tewg *et al.* [9], lower zirconia doping concentrations in tantala were observed to suppress crystallization, with a highest crystallization temperature measured from a sample with $Zr/(Zr + Ta) \simeq 0.33$. Investigations are currently underway for thin films with varying levels of zirconia doping concentrations.

In conclusion, we have presented a detailed study on the effect of annealing on zirconia-doped tantala amorphous thin films using a combination of experimental data and modeling routines. Upon annealing, there are subtle changes observed in the SRO, but the most significant change is the increase in the IRO. The GIPDF measurement method and the modeling scheme employed in this work represent a significant step forward for the detailed study of the atomic structure of amorphous thin films, providing a powerful tool capable of accurately capturing subtle changes in the atomic structure up to 15 Å. In order to reduce coating thermal noise for Advanced LIGO +, our results and analysis indicate that an optimized zirconia doping concentration of $Zr/(Zr + Ta) \simeq 0.33$ for a coating deposited in a similar way will further suppress crystallization and also increase the ratio of CS to ES polyhedra,

and allow a maximum reduction of mechanical loss. Future modeling experiments are planned to directly compute the mechanical loss of these structures [31], which will help to quantify the change in the ratio of CS to ES polyhedra has on mechanical loss. In addition, further study of other materials that increase the ratio of CS to ES polyhedra and crystallization temperature will be important to identify other low mechanical loss coating materials, and is the subject of ongoing research.

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