

Phys 2053: Homework V

due February 17, 2016

Schrödinger Equation

1. (3 p) Let us consider operators and eigenfunctions. Consider the functions

$$\begin{aligned}\phi_1(x) &= \cos kx \\ \phi_2(x) &= \sin kx\end{aligned}\tag{1}$$

and decide if those functions are eigenfunctions of the momentum operator. If they are not, then find a linear combination of the two functions, which is an eigenfunction of the momentum operator.

2. (3 p) An electron moves in a one-dimensional lattice with the separation between adjacent atoms being equal to a ,

(a) Write down the momentum eigenvalue equation for the electron.

(b) Find the general form of the solution of the eigenvalue equation.

(c) By requiring that the electron's wave function $\Psi(x)$ satisfies the periodic boundary condition

$$\Psi(a) = \Psi(0)\tag{2}$$

determine the possible values of the momentum of the electron.

2. (4 p) An electron with a kinetic energy 4.0 eV is incident upon a potential barrier of height 5.0 eV and width 0.1 nm (similar to the barrier illustrated in Morrison Fig. 3.6). Estimate the probability that the electron will pass through the barrier.