

Ex : A car of **$m=1600$ kg** travels at a constant speed of **$v=20$ m/s** along a flat, circular road of radius **$R=190$ m**. What is the minimum value of μ_s that will prevent the car from slipping?

○ Begin with free-body diagram of the car.

○ Now use Newton's 2nd law.

$$\Sigma F_y = ma_y : \quad N - mg = ma_y = 0, \quad N = mg$$

$$\Sigma F_r = ma_r : \quad f_s = \frac{mv^2}{R}, \quad f_s^{max} = \mu_s N = \mu_s mg$$

$$\Rightarrow \mu_s mg = \frac{mv^2}{R}, \quad \mu_s = \frac{v^2}{gR}$$

○ Now plug in the known parameters.

$$\mu_s = \frac{(20 \text{ m/s})^2}{(9.81 \text{ m/s}^2)(190 \text{ m})} = 0.21$$

○ Note two things:

1). $\mu_s \propto v^2$; μ_s increases with velocity.

2). μ_s does not depend on the vehicle's mass.