## Math 4620/5620

## Practice problem for the final

Consider the following linear program (from HW2):

$$
\begin{aligned}
& \max \quad x_{1}+2 x_{2}-x_{3} \\
& \text { s. t. } 2 x_{1}+2 x_{2}-2 x_{3} \leq 10 \\
& 3 x_{1}-2 x_{2}+2 x_{3} \leq 5 \\
& x_{1}-4 x_{2}+x_{3} \leq 10 \\
& x_{1}, x_{2}, x_{3} \geq 0
\end{aligned}
$$

and the simplex tableau after several iterations:

|  | $x_{1}$ | $x_{2}$ | $x_{3}$ | $x_{4}$ | $x_{5}$ | $x_{6}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $z$ | 1 | 0 | -1 | 1 | 0 | 0 | 10 |
| $x_{2}$ | 1 | 1 | -1 | $\frac{1}{2}$ | 0 | 0 | 5 |
| $x_{5}$ | 5 | 0 | 0 | 1 | 1 | 0 | 15 |
| $x_{6}$ | 5 | 0 | -3 | 2 | 0 | 1 | 30 |
|  |  |  |  |  |  |  |  |

Make a single change in the original data (that is, matrice $A$ and vectors $b, c$ ) so that the new problem has an optimal solution (no simplex iterations are necessary to answer the question).

