## Applications of Linear Programming

## 1. Facility Location problem.

A company is considering opening warehouses in four cities: New York, Los Angeles, Chicago, and Atlanta. Each warehouse can ship 100 units per week. The weekly fixed cost of keeping each warehouse open is $\$ 400$ for New York, $\$ 500$ for Los Angeles, $\$ 300$ for Chicago, and $\$ 150$ for Atlanta. Region 1 of the country requires 80 units per week, region 2 requires 70 units per week, and region 3 requires 40 units per week. The costs (including production and shipping costs) of sending 1 unit from a plant to a region are shown in the following table:

| FROM | TO |  |  |
| :---: | :---: | :---: | :---: |
|  | Region 1 | Region 2 | Region 3 |
| New York | $\$ 20$ | $\$ 40$ | $\$ 50$ |
| Los Angeles | $\$ 48$ | $\$ 15$ | $\$ 26$ |
| Chicago | $\$ 26$ | $\$ 35$ | $\$ 18$ |
| Atlanta | $\$ 24$ | $\$ 50$ | $\$ 35$ |

We wish to meet weekly demands at minimum cost, subject to the preceding information and the following restrictions:

1. If the New York warehouse is opened, then the Los Angeles warehouse must be opened.
2. At most two warehouses can be opened.
3. Either the Atlanta or the Los Angeles warehouse must be opened. Formulate a linear integer program that can be used to minimize the weekly costs of meeting demands.
